

SOME INEQUALITIES FOR GENERALIZED FRACTIONAL INTEGRAL OPERATORS ON GENERALIZED MORREY SPACES

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Abstract. Boundedness of generalized fractional integral operators on generalized Morrey spaces and their related results were shown by many authors. We consider one of their results in a wider framework. Moreover, we show some inequalities for another operator on generalized fractional integrals on generalized Morrey spaces.

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