

## ON AN EXTENDED HADAMARD MAXIMUM DETERMINANT PROBLEM

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*Abstract.* Motivated by the Hadamard maximum determinant problem we study the quantities  $a_{m,n} = \max \det(AA^T)$  where  $A$  is a  $m \times n$  matrix with entries 1 and  $-1$ . We find the exact values of  $a_{2,n}$  and  $a_{3,n}$  and for a general  $m$  we give upper and lower bounds for  $a_{m,n}$ .

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