

## SOME MAJORIZATION INEQUALITIES FOR CONVEX FUNCTIONS OF SEVERAL VARIABLES

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*Abstract.* The purpose of this note is to prove some weak majorization inequalities involving convex functions of several variables. A sub-additive inequality for separately matrix convex functions is also proved.

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