

## GLOBAL ESTIMATES FOR THE MAXIMAL OPERATOR AND HOMOTOPY OPERATOR

YUMING XING AND SHUSEN DING

*Abstract.* In this paper, we develop some estimates for the Hardy-Littlewood maximal operator and the sharp maximal operator. We also establish  $L^s$ -norm inequalities related to the composite operators.

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