ON A JENSEN–HOSSZÚ EQUATION, II

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Abstract. We solve functional equation of the form

$$f(x+y-xy) + f(xy) = 2f\left(\frac{x+y}{2}\right)$$

in the class of functions transforming the unit interval into the space of all reals. We also prove that this equation is stable in the Hyers-Ulam's sense.

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