

MARTINGALE VERSIONS OF YANO'S EXTRAPOLATION INEQUALITIES

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Abstract. In the paper we obtain some martingale versions of extrapolation theorems of Yano type by employing the technique of atomic decomposition in some Orlicz martingale spaces. Some variant extrapolation inequalities are also given.

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