

CHARACTERIZATION OF UNITARY OPERATORS BY ELEMENTARY OPERATORS AND UNITARILY INVARIANT NORMS

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Abstract. In this work we characterize unitary operators via inequalities of elementary operators with unitarily invariant norms.

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