

ESTIMATES FOR BERNSTEIN TYPE OPERATORS

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Abstract. We prove the existence of a sequence of linear positive bounded polynomial operators on $C[0, 1]$ which preserve the functions $e_0(x) = 1$ and $e_2(x) = x^2$. An extremal property and quantitative estimates are given.

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