

A PART-METRIC VARIANT OF NEWTON'S INEQUALITIES

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Abstract. This note gives a part-metric variant of Newton's inequalities. A particular case proved useful recently in the study of difference equations involving ratios of elementary symmetric polynomials.

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1. Introduction

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