

FACTORIZATION OF FACTORIALS AND A RESULT OF HARDY AND RAMANUJAN

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Abstract. We obtain an explicit approximation for the sum of prime powers in the factorization of $n!$ into prime numbers. This reproves, as more as gives an explicit version to, a well-known result of Hardy and Ramanujan concerning the summation $\sum_{k \leq n} \Omega(k)$.

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