

## THE MULTIPLICATION OPERATOR FROM MIXED-NORM TO $n$ -TH WEIGHTED-TYPE SPACES ON THE UNIT DISK

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*Abstract.* Let  $H(\mathbb{D})$  be the space of analytic functions on  $\mathbb{D}$  and  $u \in H(\mathbb{D})$ . The boundedness and compactness of the multiplication operator from mixed-norm space to  $n$ th weighted-type spaces on the unit disk are investigated in this paper.

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