

INTERPOLATION OF POSITIVE OPERATORS ON VARIABLE LEBESGUE SPACES

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Abstract. We prove an interpolation theorem for integral operators with positive kernel on the variable Lebesgue spaces. As an application we show that the set of exponents for spaces on which the Hardy-Littlewood maximal operator is bounded is convex.

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