FUGLEDE–PUTNAM'S THEOREM FOR *W*–HYPONORMAL OPERATORS

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Abstract. An asymmetric Fuglede-Putnam's Theorem for w-hyponormal operators and dominant operators is proved, as a consequence of this result, we obtain that the range of the generalized derivation induced by the above classes of operators is orthogonal to its kernel.

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