

## SOME NEW BOUNDS FOR THE GENERALIZED TRIANGLE INEQUALITY

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*Abstract.* In this paper we present some new inequalities in normed linear spaces which much improve the triangle inequality. Our results refine and generalize the corresponding ones obtained by Mitani et al. [On sharp triangle inequalities in Banach spaces, *J. Math. Anal. Appl.* **336** (2007) 1178–1186].

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