

## ON SOME HERMITE–HADAMARD–FEJÉR INEQUALITIES FOR $(k, h)$ –CONVEX FUNCTIONS

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*Abstract.* We introduce the class of  $(k, h)$ -convex functions defined on  $k$ -convex domains, and we prove some new inequalities of Hermite-Hadamard and Fejér type for such mappings. This generalizes results given for  $h$ -convex functions in [1, 17], and for  $s$ -Orlicz convex mappings in [4].

*Mathematics subject classification (2010):* Primary: 26A51, 26D15; Secondary: 52A30.

*Keywords and phrases:* Generalized convexity, Hermite-Hadamard's inequality, Fejér's inequality.

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