

CHARACTERIZATION OF THE INTERMEDIATE VALUES OF THE TRIANGLE INEQUALITY

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Abstract. We shall present a norm inequality which gives the all intermediate values of the triangle inequality. As an application of it, we shall prove two kinds of norm inequalities in [8] and [12].

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