

## ON THE INTERLACING OF CYLINDER FUNCTIONS

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*Abstract.* Necessary and sufficient conditions for the interlacing of the zeros of cylinder functions and their derivatives of different orders are given.

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