

NOTE ON KATO'S TYPE INEQUALITY

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Abstract. The main purpose of this note is to prove a Kato's type inequality for a generalized Schrödinger operator \mathcal{A} . As an application, we present the L^∞ -uniqueness of \mathcal{A} .
Mathematics subject classification (2010): 35J10, 60J60.

Keywords and phrases: Kato inequality, Schrödinger operator, uniqueness.

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