NEW SHARP ESTIMATES OF THE GENERALIZED
EULER–MASCHERONI CONSTANT

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Abstract. The aim of this paper is to establish new sequences which converge towards the Euler-Mascheroni constant. Our results solve some open problems posed by Berinde [A new generalization of Euler's constant Creat. Math. Inform. 18 (2009) no. 2 123–128] and extend some results of DeTemple, [A quicker convergence to Euler's constant Amer. Math. Monthly 100 (1993) 468–470] and Sîntămărian [A generalization of Euler's constant, Numer. Algorithms 46 (2007), 141–151].

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