

MIXED RADIAL BLASCHKE–MINKOWSKI HOMOMORPHISMS AND COMPARISON OF VOLUMES

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Abstract. In this paper we consider a Busemann-Petty type problem for mixed radial Blaschke-Minkowski homomorphisms.

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