UNIFORM BOUNDEDNESS OF CONDITIONAL EXPECTATION OPERATORS ON A BANACH FUNCTION SPACE

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Abstract. Let X be a Banach function space over a nonatomic probability space. The quasi-Banach space weak–X is defined in a natural way. We give some necessary and sufficient conditions on X for all the conditional expectation operators to be uniformly bounded operators from X into weak–X.

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