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# ON THE RATIO BETWEEN SUCCESSIVE RADII OF A SYMMETRIC CONVEX BODY

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*Abstract.* In this note we study the upper bound for the ratio between the so called successive inner and outer radii of a 0-symmetric convex body $K$. This problem was studied by Perel'man and Pukhov and it is a natural generalization of the classical results of Jung and Steinhagen.

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