

## WILKER AND HUYGENS TYPE INEQUALITIES FOR THE LEMNISCATE FUNCTIONS, II

CHAO-PING CHEN

*Abstract.* In this paper, we establish new Wilker and Huygens type inequalities for the Lemniscate functions.

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