

## HARDY TYPE INEQUALITIES FOR FRACTIONAL AND $q$ -FRACTIONAL INTEGRAL OPERATORS

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**Abstract.** Hardy type inequality for different fractional integral operators with sharp constants on finite intervals are given.

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