

ON MONOTONICITY PROPERTIES OF THE L_p -CENTROID BODIES

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Abstract. Monotonicity properties for the quermassintegrals and dual quermassintegrals of the L_p -centroid bodies are proved and equality cases are investigated.

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