

SOME HARDY INEQUALITIES ON HALF SPACES FOR GRUSHIN TYPE OPERATORS

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Abstract. We prove some sharp Hardy type inequalities on half spaces for Grushin type operators like $\Delta_x + (1 + \gamma)^2 |x|^{2\gamma} \Delta_y$ with $\gamma > 0$.

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