

MAXIMUM PRINCIPLES FOR A CLASS OF LINEAR ELLIPTIC EQUATIONS OF EVEN ORDER

CRISTIAN-PAUL DANET AND ANITA MARENO

Abstract. In this paper we define several types of functions on the solution to a class of linear elliptic equations of even order. We establish that these functions satisfy a classical maximum principle. As a consequence we obtain uniqueness results and bounds on various quantities of interest.

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