ASYMPTOTIC EXPANSIONS OF THE MULTIPLE QUOTIENTS
OF GAMMA FUNCTIONS WITH APPLICATIONS

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Abstract. Asymptotic expansions of the multiple quotients of two gamma functions are obtained and analyzed. We apply these results to the hypergeometric function and central multinomial coefficient which leads to the new approximation formulas.

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