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# ON MEAN VALUES OF FOURIER TRANSFORMS

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*Abstract.* We show that there exists a sequence $\{n_k, k \geqslant 1\}$ growing at least geometrically such that for any finite non-negative measure $\nu$ such that $\widehat{\nu} \geqslant 0$, any $T > 0$,

$$\int_{-2^{n_k}T}^{2^{n_k}T} \widehat{\nu}(x)\mathrm{d}x \ll_\varepsilon T\, 2^{2^{(1+\varepsilon)n_k}} \int_{\mathbb{R}} \left|\frac{\sin xT}{xT}\right|^{n_k^2} \nu(\mathrm{d}x).$$

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