

NEW CONVERSES OF THE JESSEN AND LAH-RIBARIČ INEQUALITIES

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Abstract. New converses of the Jessen and Lah-Ribarič inequalities for continuous convex functions with applications to means, the Hölder inequality, the Hadamard inequality, and the inequalities of Giaccardi and Petrović are given.

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