

ON THE p -MIXED AFFINE SURFACE AREA

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Abstract. Some new inequalities for i -th mixed p -affine surface area are established. The results in special cases yield some of the recent results on inequalities of this type.

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