

ON SOME NEW WEIGHTED EULER SEQUENCE SPACES AND COMPACT OPERATORS

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Abstract. In this paper, we define some new Euler sequence spaces and construct Schauder basis of these spaces. Moreover, we determine their β -duals and characterize some related matrix classes. Finally, we give the characterization of some classes of compact operators on these spaces by using the Hausdorff measure of noncompactness.

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