

WEIGHTED COMPOSITION OPERATORS FROM THE LIPSCHITZ SPACE INTO THE ZYGMUND SPACE

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Abstract. In this work, we give several characterizations of the bounded and the compact weighted composition operators from the Lipschitz space into the Zygmund space.

Mathematics subject classification (2010): Primary 47B33; secondary 30H05.

Keywords and phrases: Weighted composition operator, Lipschitz space, Zygmund space.

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