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ON PROPERTIES FOR m–POLYNOMIALS OF UNIT p–BALLS

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Abstract. In this paper we study properties of 'weighted' Steiner polynomials associated to the unit p-balls. We show that the corresponding functional can be bounded just by the last but one relative quermassintegral. Then we give a general asymptotic relation between the roots of Steiner polynomials and the above mentioned polynomials. These properties will be obtained as consequences of more general results for the so called $\mathbf{m}$-polynomials.

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