SOME DYNAMIC INEQUALITIES OF HARDY TYPE ON TIME SCALES

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Abstract. In this paper we prove some new dynamic inequalities of Hardy type on time scales. The main results will be proved using algebraic inequalities, Hölder inequality and Keller's chain rule on time scales.

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