

## REVERSE HARDY-TYPE INEQUALITIES FOR SUPREMAL OPERATORS WITH MEASURES

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*Abstract.* In this paper we characterize the validity of the inequalities

$$\|g\|_{p,(a,b),\lambda} \leq c \|u(x)\| g\|_{\infty,(x,b),\mu} \|_{q,(a,b),v}$$

and

$$\|g\|_{p,(a,b),\lambda} \leq c \|u(x)\| g\|_{\infty,(a,x),\mu} \|_{q,(a,b),v}$$

for all non-negative Borel measurable functions  $g$  on the interval  $(a,b) \subseteq \mathbb{R}$ , where  $0 < p \leq +\infty$ ,  $0 < q \leq +\infty$ ,  $\lambda$ ,  $\mu$  and  $v$  are non-negative Borel measures on  $(a,b)$ , and  $u$  is a weight function on  $(a,b)$ .

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