

WEIGHTED NORM INEQUALITIES FOR BILINEAR FOURIER MULTIPLIER OPERATORS

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Abstract. In this paper, by kernel estimates of the bilinear Fourier multiple operator and the weighted theory for the bilinear singular integral operators, some weighted norm inequality with general weights are established for the bilinear Fourier multiplier operators.

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