THE STECHKIN INEQUALITY FOR FOURIER MULTIPLIERS ON VARIABLE LEBESGUE SPACES

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Abstract. We prove the Stechkin inequality for Fourier multipliers on variable Lebesgue spaces under some natural assumptions on variable exponents.

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