A GENERALIZATION OF THE HILBERT'S TYPE INEQUALITY

Gaowen Xi

Abstract. In this paper, by introducing two parameters A, B and using the Euler-Maclaurin expansion for the Riemann zeta function, we establish an inequality of a weight coefficient. Using this inequality, we derive generalizations of a Hilbert's type inequality.

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