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APPLICATIONS OF REFINED HARDY–TYPE INEQUALITIES

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Abstract. This paper is to provide the broad range of Hardy-type inequalities and their refinements for linear differential operator, Widder's derivative and more generalized fractional integral operator using convex and monotone convex functions. As special cases we give results for Saigo, Riemann-Liouville and Erdélyi-Kober fractional integral operators.

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