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ON SOLUTIONS OF A COMPOSITE TYPE FUNCTIONAL INEQUALITY

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Abstract. In the paper we consider a composite type inequality $f(x+f(x)y) \leqslant f(x)f(y)$ in the class of real continuous functions. Our paper refers to the paper [12].

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