

A REVERSE HILBERT-LIKE OPTIMAL INEQUALITY

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Abstract. We prove an inequality on positive real numbers, that looks like a reverse to the well-known Hilbert inequality, and we use some unusual techniques from Fourier analysis to prove that this inequality is optimal.

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