

ON WEIGHTED GENERALIZATION OF THE HERMITE–HADAMARD INEQUALITY

ROZARIJA JAKŠIĆ, LJILJANKA KVESIĆ AND JOSIP PEČARIĆ

Abstract. The results obtained in this paper are a correction of the main results obtained in [14], for which we also give an alternative proof and improvement. We also study some new monotonic conditions under which various generalizations of the Hermite–Hadamard inequality are valid. Furthermore, we give an improvement of the obtained results.

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