Mathematical
Inequalities
& Applications
Volume 18, Number 2 (2015), 667–685
doi:10.7153/mia-18-50

SHARP CONSTANT FOR $L^p - L^\infty$ TYPE SOBOLEV'S INEQUALITY

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Abstract. Sharp constants for $L^p - L^\infty$ type Sobolev's inequalities $\|y\|_\infty \leqslant C\|\triangle^k y\|_p$ and $\|y\|_\infty \leqslant C\|\nabla(\triangle^k y)\|_p$ are studied. The problems are solved by using Green's function and rearrangement theory.

Mathematics subject classification (2010): 26D10, 34B27, 46E35.
Keywords and phrases: Sharp constant, Sobolev's inequality, Green's function, rearrangement.

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Paper MIA-18-50