

2-HILBERT C^* -MODULES AND SOME GRÜSS' TYPE INEQUALITIES IN A -2-INNER PRODUCT SPACES

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Abstract. In this paper we generalize the concept of complex valued 2-inner product to A -valued 2-inner product, where A is a C^* -algebra. We define and study the notion of A -valued 2-inner product on right A -module E (E is a linear space) and by new definition, some Grüss type inequalities are given.

Mathematics subject classification (2010): Primary 46C99, 46C05, 46L08; Secondary 26D99.

Keywords and phrases: 2-inner products, 2-norms, inner product C^* -modules, Grüss inequalities.

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