

A MEAN VALUE THEOREM FOR THE CHEBYSHEV FUNCTIONAL

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Abstract. In the present paper we present a mean value theorem for the Chebyshev functional based on divided differences. This theorem is then used to obtain a new Chebyshev-Grüss type inequality.

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