

## CONVERGENCE IN NORM OF LOGARITHMIC MEANS OF MULTIPLE FOURIER SERIES

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*Abstract.* The maximal Orlicz space such that the mixed logarithmic means of multiple Fourier series for the functions from this space converge in  $L_1$ -norm is found.

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