

PRECISE ESTIMATES OF BOUNDS ON RELATIVE OPERATOR ENTROPIES

SHIGERU FURUICHI

Abstract. Recently, Zou obtained the generalized results on the bounds for Tsallis relative operator entropy. In this short paper, we give precise bounds for Tsallis relative operator entropy. We also give precise bounds of relative operator entropy.

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