THE SHARP UPPER BOUND FOR THE RATIO BETWEEN
THE ARITHMETIC AND THE GEOMETRIC MEAN

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Abstract. In this note we present the sharp upper bound for the ratio between the arithmetic and
the geometric mean for concave sequences. In this way the sharp reverse of the Arithmetic-
Geometric Mean Inequality is obtained.

Keywords and phrases: Arithmetic-geometric mean inequality, concave sequence.

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