

SOME IMPROVEMENTS OF THE POPOVICIU, BELLMAN AND DIAZ—METCALF INEQUALITIES VIA SUPERQUADRATIC FUNCTIONS

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Abstract. We give refinements of the generalized Bellman and Diaz–Metcalf inequalities for isotonic linear functionals by using the concept of superquadratic functions. Further, we give refinements of the generalized Bellman and Diaz–Metcalf inequalities for time scales integrals as applications of the above obtained inequalities for isotonic linear functionals. Moreover we give refinements of the Aczél and Popoviciu inequalities for time scales integrals.

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REFERENCES

- [1] S. ABRAMOVICH, G. JAMESON AND G. SINNAMON, *Inequalities for averages of convex and superquadratic functions*, Math. Inequal. Appl., **5**, 4 (2004), Article 91, 14 pp.
- [2] S. ABRAMOVICH, G. JAMESON AND G. SINNAMON, *Refining Jensen's inequality*, Bull. Math. Soc. Sci. Math. Roumanie (N.S.), **47** (95), 1–2 (2004), 3–14.
- [3] M. ANWAR, R. BIBI, M. BOHNER AND J. PEČARIĆ, *Integral inequalities on time scales via the theory of isotonic linear functionals*, Abstr. Appl. Anal., **2011**, (2011), Art. ID 483595, 16 pp.
- [4] S. BANIĆ, *Superquadratic functions*, PhD thesis, University of Zagreb, Zagreb, Croatia, 2007. In Croatian.
- [5] S. BANIĆ AND S. VAROŠANEC, *Functional inequalities for superquadratic functions*, Int. J. Pure Appl. Math., **43**, 4 (2008), 537–549.
- [6] J. BARIĆ, R. BIBI, M. BOHNER AND J. PEČARIĆ, *Time scales integral inequalities for superquadratic functions*, J. Korean Math. Soc., **50**, 3 (2013), 465–477.
- [7] M. BOHNER AND G. SH. GUSEINOV, *Multiple Lebesgue integration on time scales*, Adv. Difference Equ., **2006**, (2006), Art. ID 26391, 13 pp.
- [8] J. E. PEČARIĆ, F. PROSCHAN AND Y. L. TONG, *Convex Functions, Partial Orderings, and Statistical Applications*, volume 187 of Mathematics in Science and Engineering, Academic Press Inc., Boston, MA, 1992.